Ab Initio Investigation of the Electronic and Geometric Structure of Magnesium Diboride, MgB₂

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Employing multireference variational (MRCI) and coupled cluster (CC) methods combined with quadruple- ζ quality correlation-consistent basis set, we have studied 36 states of the magnesium diboride (MgB₂) molecule as well as 17 states of the experimentally unknown diatomic MgB. For all states of MgB₂, we report geometries, atomization energies, and dipole moments, while for the first 5 states, potential energy profiles have been also constructed. The ground state is formally of ¹A₁ V-shaped symmetry with an atomization energy of 108.1(109) kcal/mol at the MRCI(MRCI + Davidson correction) level. The first excited state (³B₁) is less than 1 kcal/mol above the \tilde{X}^1A_1 state, with the next state of linear Mg–B–B geometry ($\tilde{b}^3\Sigma^-$) located 10 kcal/mol higher. In all states, bent or linear, the bonding is complicated and unconventional because of the extraordinary bonding agility of the boron atom(s).

1. Introduction

In 2001, Jun Akimitsu's group¹ discovered that the simple compound magnesium diboride (MgB₂) becomes superconducting at the transition temperature $T_c = 39$ K, almost twice as large compared to the highest T_c among the intermetallics, namely, that of Nb₃Ge ($T_c = 23$ K).² Given the chemical simplicity of MgB₂ as well as its simple crystal structure,^{1,3} the natural abundance of its constituent elements, and therefore the prospects for plausible applications, this was indeed a remarkable discovery. The enthusiastic response of the scientific community was testified to by a series of experimental⁴ and theoretical⁵ publications.

It is worthwhile to recall at this point that the elements Mg and B have played a fundamental role in the development of "pure and applied chemistry" as only the names of "Grignard reagent" (RMgX) and "boron hydrides" (B_xH_y) suggest.⁶ And although MgB₂ has been well-characterized since the early fifties,³ until now nobody suspected its unusual properties. Experimenters using different techniques have already established a variety of sometimes "conflicting" properties, for example, the existence of two superconducting gaps in MgB₂ which had not been seen before in any material.²

Obviously, all the above characteristics of MgB₂ refer to the solid state. On the other hand, there are three very recent theoretical ab initio works on the isolated noninteracting MgB₂ molecule. The first one by Ercoç in 2003 was conducted at a very low level of theory;⁷ in 2004, Yang et al.⁸ calculated 9 states (6 linear and 3 bent) around equilibrium using the QCISD/ $6-311G^*$ and CCSD(T)/cc-pVTZ methods predicting different ground states, ³B₁ and ¹A₁, respectively. However, on the basis of their CCSD(T) results, they concluded that the ground state is of ¹A₁ symmetry with the ³B₁ state 412 cm⁻¹ higher. A few months later, Lee and Wright⁹ published the investigation of 21 states of MgB₂ around equilibrium using a variety of methods, MP2, DFT(B3LYP), QCISD, UCCSD(T), and RCCSD-

(T), employing a 6-311+G (3df) basis set. Not all 21 states have been calculated at all levels of theory, only at MP2. Ten of the 21 states have been calculated at the DFT level with conflicting results as compared to the MP2 values. At the QCISD and UCCSD(T) levels, they calculated 3 states, again with conflicting results between these 2 methods. Now, at the RCCSD(T) level and using a correlation-consistent aug-ccpVQZ basis, they obtained the first 4 states around equilibrium. Then, they recalculated these 4 states by including core functions on B and Mg, but at the geometry of the previous level. Finally, they also performed MRCI/aug-cc-pVQZ/RCCSD(T)/aug-ccpVQZ, i.e., single-point calculations, for these 4 lowest states. At this level of theory, Lee and Wright⁹ concluded as well that the ground state is of ${}^{1}A_{1}$ symmetry with the $\tilde{a}{}^{3}B_{1}$ about 0.4 kcal/mol higher.⁹

Motivated by the remarkable properties of crystalline MgB_2 and the somehow conflicting theoretical results reported so far,^{8,9} we herein report ab initio calculations using multireference and coupled-cluster methods in conjunction with quantitative correlation-consistent basis sets. In both methods, the symmetry of the ground state seems to be ${}^{1}A_{1}$ (but, see below).

We have examined a total of 36 states, reporting energetics, dipole moments, geometric and spectroscopic parameters, and Mulliken densities. In addition, for the first 5 states, we have constructed potential energy profiles of the corresponding potential surfaces, while some emphasis is given in explaining the bonding with the help of simple valence-bond-Lewis (vbL) diagrams.

In section 2, we define the computational procedure followed; in section 3, we present our results on the diatomics MgB and B_2 and on the triatomic MgB₂, and in section 4, some final remarks and comments are presented.

2. Computational Procedure

For the Mg and B atoms, the correlation-consistent basis by Dunning¹⁰ of quadruple cardinality, cc-pVQZ = 16s12p3d2f1g and 12s6p3d2f1g, respectively, were employed through all

calculations. Both sets were generally contracted to [6s5p3d2f1g/ Mg 5s4p3d2f1g/B], amounting to 169 spherical Gaussian functions for the MgB₂ system.

Our general approach is the complete active space selfconsistent field (CASSCF) method, extended to the single and double replacements out of the zeroth-order CASSCF wave function (CASSCF + 1 + 2 = MRCI), to account for "dynamical" correlation. Our reference space is built by allotting the 8 (chemically) active electrons of MgB_2 (3s² on Mg and 2s²2p¹ on each B atom) among 12 orbital functions (3s and 3p on Mg + 2s and 2p on B's). The ensuing CASSCF wave function expansions range from 12 776 (⁵B₂; BMgB) to 28 376 (³B₂; BMgB) configuration functions (CF), with MRCI spaces ranging from 111×10^6 (MgBB; $^{1}\Sigma^{-}$) to 202×10^6 (MgBB; ${}^{3}\Sigma^{-}$) CFs. By applying the internal contraction (icMRCI) approximation,¹¹ the number of CFs is reduced by more than an order of magnitude, thus making the calculations feasible. Size nonextensivity errors do not exceed 2 mh at the icMRCI level, reduced to about 0.5 mh by including the Davidson correction for quadruples (+Q).

For the four lowest states, \tilde{X}^1A_1 (BMgB), ${}^{3}B_1$ (BMgB), ${}^{3}\Sigma^{-1}$ (MgBB), and ${}^{5}\Sigma^{-}$ (MgBB), the coupled-cluster single reference + singles + doubles + perturbative connected triples method [RCCSD(T)] as implemented in MOLPRO¹² was also used. Note that both SCF and CASSCF orbitals were used for the construction of the single reference function. For the ¹A₁ state only, Møller-Plesset MP2 and MP4 calculations were also tried with the harmonic frequencies obtained at the MP2/cc-pVQZ level of theory.

Finally, concerning the diatomic molecules MgB and B₂, we have examined 17 and 5 states, respectively, at the ic-MRCI/ cc-pVQZ level and within the spirit outlined above.

3. Results and Discussion

A. The Diatomics MgB and B₂. In the present work, two geometrical isomers of MgB2 are examined, namely, B-Mg-B and Mg-B-B: Both can be thought of as products of the interaction channels MgB + B or $Mg + B_2$. Therefore, for a better understanding of MgB₂, the study of both diatomics MgB and B₂ is rather mandatory.

It is rather surprising that no experimental results are available for MgB. Theoretically, we are aware of only two publications on MgB by Boldyrev et al.13 and by Machado and co-workers.14 The former authors investigated the first four states $X^2\Pi$, $A^2\Sigma^+$, ${}^{4}\Pi$, and ${}^{4}\Sigma^{-}$ and a higher excited state of ${}^{2}\Pi$ symmetry around equilibrium, in a variety of single reference methods, namely, MP2(full)/6-311+G*, QCISD(T)/6-311+G(2df), and MP4/6-311+G*//MP2/6-311+G*. Machado et al.¹⁴ examined the first two states of BeB, MgB, and CaB using a (truncated) MRCISD/ 6-311+G(3d1f).

On the contrary, B_2 is a well-explored molecule both experimentally¹⁵ and theoretically.¹⁶ Nevertheless, for reasons of uniformity and completeness, the five lowest states of the B2 molecule are currently examined at the MRCI/cc-pVQZ level.

The MRCI energy splittings of Mg $[^{1}P, ^{3}P(3s^{1}3p^{1}) \leftarrow ^{1}S$ - $(3s^2)$] and B atoms $[{}^4P(2s^12p^2) \leftarrow {}^2P(2s^22p^1)]$ are in excellent agreement with experiment (in parentheses¹⁷): 2.603 (2.714), 4.318 (4.346), and 3.591 (3.571) eV, respectively. These three excited states are actively involved in the calculated states of MgB, B₂, and MgB₂.

MgB. Table 1 lists the energetics, the usual spectroscopic parameters, and the dipole moments of 17 states of MgB, spanning an energy range of about 4.2 eV, correlating adiabati-



Figure 1. Potential energy curves of 17 states of the MgB molecule at the MRCI/cc-pVQZ level of theory. All energies have been shifted by $+224 E_{\rm h}$.

cally to Mg(^{1}S) + B(^{2}P , ^{4}P), Mg(^{3}P) + B(^{2}P), and Mg(^{3}P) + $B(^{4}P)$ (16⁶ Σ^{-}). Corresponding potential energy curves (PECs) are plotted in Figure 1. Table 2 presents leading CASSCF configurations and Mulliken atomic populations of the first four states of MgB (X² Π , A² Σ^+ , 2⁴ Σ^- , and 3⁴ Π). The valence-bond-Lewis (vbL) bonding diagrams of these four states based on their CFs and population densities are shown below.

$$Mg^{(1)} = Mg^{-1}$$

$$Mg^{(1)} = Mg^{-1}$$

$$Mg^{(2)} = Mg^{-1}$$

$$\mathbf{C} = \mathbf{M} \mathbf{g} \mathbf{H} \mathbf{g} \mathbf{H} \mathbf{H} \mathbf{g} \mathbf{$$

 $Mg(^{1}S)$ $A^2\Sigma^+$ $B(^{2}P; M=0)$

$$\underbrace{\bigcirc}_{3s} \underbrace{\bigcirc}_{2s} \underbrace{\bigcirc}_{2s} + \underbrace{\bigcirc}_{2s} \underbrace{\bigcirc}_{s} \underbrace{\bigcirc$$

 $2^{4}\Sigma^{-}(1)$

$$Mg(^{3}P; M=\pm 1) \quad B(^{2}P; M=\mp 1)$$

 $Mg(^{3}P; M=0) B(^{2}P; M=\pm 1)$

The ground state of MgB is of ${}^{2}\Pi$ symmetry with a binding energy and internuclear distance of $D_{\rm e} = 11.85$ (12.7) kcal/ mol and $r_e = 2.3862$ (2.383) Å, respectively, at the MRCI-

TABLE 1: Absolute Energies E (hartree), Bond Lengths r_e (Å), Binding Energies D_e (kcal/mol) with Respect to the Adiabatic Fragments, Harmonic Frequencies and Anharmonic Corrections ω_e , $\omega_e x_e$ (cm⁻¹), Rotational Vibrational Couplings α_e (cm⁻¹), Centrifugal Distortions \overline{D}_e (cm⁻¹), Mulliken Charges on $B q_B$, Dipole Moments μ (debye), and Energy Separations T_e (kcal/mol) of the MgB Molecule at CASSCF, MRCI, and MRCI+ Q^b /cc-pVQZ Levels. Other Theoretical Results Are Also Included.

state	method	-E	r _e	$D_{\rm e}$	$\omega_{\rm e}$	$\omega_{\rm e} x_{\rm e}$	$\alpha_e(10^{-3})$	$\bar{D}_{\rm e}(10^{-6})$	$-q_{\rm B}$	$\langle \mu \rangle / \mu_{\mathrm{FF}}^{c}$	$T_{\rm e}$
$X^2\Pi$	CASSCF	224.211593	2.4423	2.69	310.9	12.4	10.6	2.18	0.24	1.86/1.86	0.0
	MRCI	224.267947	2.3862	11.85	365.9	6.14	6.80	1.80	0.31	2.38/2.39	0.0
	MRCI+Q	224.27062	2.383	12.7						/2.44	0.0
	MP2(full)/6-311+G* d	224.351223	2.473		269						0.0
	$QCISD(T)/6-311+G(2df)^d$	224.25419	2.390	10.8							0.0
$A^2\Sigma^+$	CASSCF	repulsive									0.0
	MRCI	224.252702	2.7515	2.28	192.3	10.6	12.1	2.79	0.04	-0.42/-0.41	9.57
	MRCI+Q	224.25481	2.730	2.83						/-0.31	9.92
	MP2(full)/6-311+G* d	repulsive									
	$QCISD(T)/6-311+G(2df)^d$	224.23962	2.775	1.7							9.1
$2^{4}\Sigma^{-}(1)$	CASSCF	224.183512	2.1605	47.97	525.5	3.20	4.44	1.59	0.35	3.37/3.37	17.6
	MRCI	224.235687	2.1259	51.98	554.9	3.54	4.54	1.57	0.39	3.85/3.84	20.2
	MRCI+Q	224.23792	2.126	52.2						/3.87	20.5
	MP2(full)/6-311+G* d	224.32603	2.117		568						15.8
	$QCISD(T)/6-311+G(2df)^{d,e}$	224.22221									20.1
$3^{4}\Pi(1)$	CASSCF	224.182164	2.2703	45.33	446.7	1.66	6.20	1.62	0.40	2.04/2.04	18.5
	MRCI	224.235411	2.2769	51.61	474.8	0.01	2.52	1.41	0.37	1.98/1.92	20.4
	MRCI+Q	224.23820	2.276	52.3						/1.92	20.3
	MP2(full)/6-311+G* ^d	224.33561	2.263		510						9.8
	$QCISD(T)/6-311+G(2df)^{d,e}$	224.22283									19.7
$4^{2}\Sigma^{-}(1)$	CASSCF	224.153555	2.1973	26.07	493.2	3.40	3.72	1.63	0.47	2.13/2.13	36.4
	MRCI	224.209085	2.1496	35.04	517.0	5.42	12.3	1.71	0.47	2.64/2.80	36.9
	MRCI+Q	224.21202	2.149	35.9						/2.81	37
$5^{2}\Pi(2)$	CASSCF ^{<i>i</i>}	224.14056	2.338	20.1	424.5	4.03	3.84	1.51	0.35	1.89/2.05	44.6
	MRCI	224.20685	2.305	33.7	458.1	4.39	4.98	1.42	0.37	2.12/2.03	38.3
-2.4.(4)	MRCI+Q	224.2116	2.308	35.6	1.00 0		1.00	1.01		/2.05	37
$6^2\Delta(1)$	CASSCF	224.13460	2.203	17.9	460.6	5.80	4.80	1.84	0.23	2.02/2.59	48.3
	MRCI	224.20383	2.151	31.8	521.0	5.37	6.46	1.66	0.35	3.25/3.30	40.2
$\pi^2\Sigma^{\pm}(0)$	MRCI+Q	224.2083	2.157	33.2	270.2	11.0	0.00	0.01	0.00	/3.35	39 52 7
$7^{2}\Sigma^{+}(2)$	CASSCE	224.12/6/	2.264	13.4	3/9.3	11.0	9.29	2.31	0.20	1.75/1.93	52.7
	MRCI	224.19086	2.231	23.7	404.8	/.8/	8.76	2.22	0.25	2.37/2.37	48.4
$\rho^2 \Pi(2)$	MRCI+Q	224.1940	2.233	24.7	202.0	6.69	2.52	1.10	0.10	/2.33	48
8-11(3)	CASSCF ⁶	224.11280	2.131	4.74	202.8	0.08	3.33	1.10	0.18	0.87/0.07	02.0 55.7
	MRCI – 0	224.17914	2.724	10.4	200.0	0.96	1.80	1.30	0.04	/_0.50	53.7
$0^2\Sigma^+(2)$	CASSCE	224.1041	2.712	-0.28					0.07	0.55/0.15	54
9 2 (3)	MRCI	224.10555	2 596	0.38	357.8	8 87	4.40	1.14	0.07	0.35/0.13	64.3
	MRCI+0	224.10040	2.570	9.5	557.0	0.07	7.70	1.14	0.15	/0.58	63
$10^{4}\Sigma^{-}(2)$	CASSCE	224.1703	2.546	4 32	414.2	28.8	16.4	2 43	0 39	3 24/3 55	71.2
10 2 (2)	MRCI	224.05020	2.100	26.9	618.1	6.10	3 15	1 35	0.39	3 83/3 86	67.9
	MRCI+0	224 1636	2.101	29.0	010.1	0.10	5.15	1.55	0.07	/3.89	67
$11^4\Lambda(1)$	initer i Q	repulsive	2.101	27.0						/5.02	07
$12^{4}\Sigma^{+}(1)$		repulsive									
$13^{4}\Pi(2)$	CASSCF	repulsive									
- ()	MRCI	224.15321	5.000	0.22					0.00	-0.08/-0.11	72.0
	MRCI+O	224.1555	4.799	0.26						/-0.14	72
$14^{4}\Sigma^{+}(2)$		repulsive									
$15^{4}\Pi(3)$	CASSCF	repulsive									
	MRCI	224.11855	3.945	1.04					0.02	0.08/0.07	93.7
	MRCI+Q	224.1196	3.881	1.29						/0.14	95
$16^{6}\Sigma^{-}(1)$	CASSCF	224.08667	2.303	49.8	437.3	2.44	3.88	1.57	0.49	3.00/3.00	78.4
	MRCI	224.11443	2.293	58.2	441.9	2.49	3.93	1.57	0.48	3.03/3.03	96.3
	MRCI+O	224.1151	2.294	58.5						/3.03	98

^{*a*} Internally contracted MRCI. ^{*b*} +Q refers to the multireference Davidson correction. ^{*c*} $\langle \mu \rangle$ calculated as expectation value; μ_{FF} calculated by the finite field method. ^{*d*} Ref 13. ^{*e*} QCISD(T)/6-311+G(2df)/MP2(full)/6-311+G*. ^{*f*} State-averaged CASSCF.

(+Q) level. According to diagram 1, this rather weak bonding of the X ²Π state is the result of a charge transfer from Mg to B via the σ frame and from B to Mg through the π frame, amounting to a total electron transfer to the B atom of about 0.2 e⁻ and a σ , ¹/₂ π (one electron) bonding character. The next two states, $2^{4}\Sigma^{-}$ and $3^{4}\Pi$, are strictly degenerate within the accuracy of our calculations, located about 20.5 kcal/ mol above the ground state and both correlating to Mg ($3s^{1}3p^{1}$; ³P) + B ($2s^{2}2p^{1}$; ²P). However, their electronic structure is quite different as evidenced from diagrams 3 and 4. The bonding in $^{4}\Sigma^{-}$ comprises one σ and two $^{1}/_{2} \pi$ bonds as compared to a $^{1}/_{2} \sigma$ and a $^{1}/_{2} \pi$ of the $3^{4}\Pi$ state. This is reflected in the equilibrium bond distance of $3^{4}\Pi$, which is 0.06 Å larger than the bond length of the $^{4}\Sigma^{-}$ state. Of course, both states have identical

The first excited state, $A^2\Sigma^+$ of MgB located 9.6 kcal/mol above the X state, as expected from diagram 2, is slightly or van der Waals bound by 2.28 (2.8) kcal/mol at the MRCI(+Q) level.

 TABLE 2: Leading CASSCF Configuration Functions and Mulliken Atomic Distributions of the First Four States of MgB

 Molecule

			Ν	lg		В				
state	configurations ^a	3s	$3p_z$	$3p_x$	3p _y	2s	$2p_z$	$2p_x$	$2p_y$	
$X^2\Pi$	$0.91/\sqrt{2} 1\sigma^2 2\sigma^2 (1\pi_x^1 + i1\pi_y^1)\rangle$	1.37	0.20	0.08	0.08	1.77	0.54	0.46	0.46	
$\mathrm{A}^2\Sigma^{+b}$	$0.91 1\sigma^2 2\sigma^2 3\sigma^1\rangle$	1.62	0.23	0.04	0.04	1.83	1.06	0.06	0.06	
$2^{4}\Sigma^{-}(1)$	$0.95 1\sigma^2 2\sigma^1 1\pi_x^{-1} 1\pi_y^{-1}\rangle$	0.99	0.16	0.21	0.21	1.55	0.25	0.77	0.77	
$3^{4}\Pi(1)$	$0.97/\sqrt{2} 1\sigma^2 2\sigma^1 3\sigma^1 (1\pi_x^1 + i1\pi_y^1)\rangle$	0.91	0.53	0.05	0.05	1.62	0.83	0.46	0.46	

^{*a*} Our orbital enumeration refers only to the five valence electrons, i.e., we do not count the doubly occupied four σ and two π "core" orbitals. ^{*b*} MRCI level.

TABLE 3: Absolute Energies E (hartree), Bond Lengths r_e (Å), Binding Energies D_e (kcal/mol) with Respect to the Adiabatic Atoms, Harmonic Frequencies and Anharmonic Corrections ω_e , $\omega_e x_e$ (cm⁻¹), Rotational Vibrational Couplings α_e (cm⁻¹), Centrifugal Distortions \overline{D}_e (cm⁻¹), and Energy Separations T_e (kcal/mol) of the B₂ Molecule at CASSCF, MRCI,^{*a*} and MRCI+Q^{*b*}/cc-pVQZ Levels. Experimental and Previous Theoretical Results Are Also Included.

state	method	-E	re	$D_{ m e}$	ωe	$\omega_{\rm e} x_{\rm e}$	$\alpha_{e}(10^{-2})$	$\bar{D}_{\rm e} (10^{-6})$	$T_{\rm e}$
$X^{3}\Sigma_{g}^{-}$	CASSCF	49.221045	1.6144	61.31	1017.9	8.73	1.40	6.27	0.0
5	MRCI	49.304129	1.5984	65.39	1039.2	9.03	1.44	6.38	0.0
	MRCI+Q	49.30797	1.599	65.1					0.0
	MRCI/[5s4p3d2f1 g] ^c		1.600	65.6	1041				0.0
	QCISD(T)/6-311G*d	49.28005		60.53					
	$PMP4(4)/6-311G(2df)^d$	49.28946		64.81					
	SDCI/(8s6p3d2f) ^e	49.272178	1.602	47.27					
	CASSCF/cc-pV5Z [/]	49.221420	1.6141	61.4	1018.2	8.8	1.40		
	MRCI/cc-pV5Z	49.306057	1.5973	65.8	1040.6	9.1	1.44		
	$CCSD(T)/cc-pCV6Z^g$	49.306/20	1.5919	64.77	1050.4				
	$CCSD(T)/cc-pCV6Z^{g,n}$	49.409725	1.5855	65.53	1059.3				
	MRCI/cc-pCV5Z ^g	49.306238	1.59/1	65.78	1040.7				
	MRCI+Q/cc-pC $\sqrt{52^s}$	49.310144	1.5973	03.33	1058.8				
	MRCI/cc-pC $\sqrt{52^{s/2}}$	49.403///	1.5902	0/.12	1052.5				
	MRCI $\pm Q/cc$ -pCV3Z ^s ^m	49.411557	1.5905	00.09	1049.5				
	WIR-AQCC/cc-pvQZ-		1.5960	60.6j	1051 2	0.251	1 <i>Ai</i>		
	expl		1.590	68.40 ± 1.4^{k}	1051.5° 1052.7^{l}	9.55	1.4		
	expt		1.590	00.49 ± 14	1052.7				
$a^5\Sigma^{-}$	CASSCE	19 221663	1.5050	131.20	1217 5	7.08	1.15	5 72	-0.39
a 20	MRCI	49 296874	1.5253	142 91	1255.1	7.00	1.15	5 79	4 55
	MRCI+0	49 29990	1.5255	143.4	1255.1	1.22	1.10	5.17	5.07
	MRCI/ $[5s4n3d2f1 g]^c$	17.27770	1.525	145	1245				4 86
	MR-AOCC/cc-pVOZ ^I		1.5250	143.68	1255				5.02
$A^3\Pi_n$	CASSCE	49,198041	1.7778	45.62	782.0	7.46	1.30	5.95	14.44
u	MRCI	49.287904	1.7545	55.09	808.2	7.44	1.31	6.03	10.18
	MRCI+Q	49.29289	1.754	55.7					9.46
	MRCI/[5s4p3d2f1 g] ^c		1.756	55.5	807				10.07
	MR-AQCC/cc-pVQZ ⁱ		1.7546	55.83	806				9.80
	expt ⁿ		1.74405		817.997	7.458	1.32	5.73	
$b^1\Delta_g$	CASSCF	49.194893	1.6365	44.90	972.9	9.87	1.49	6.32	16.41
	MRCI	49.283319	1.6172	52.30	996.9	9.88	1.52	6.46	13.06
	MRCI+Q	49.28777	1.618	52.4					12.7
	MRCI/[5s4p3d2f1 g] ^c		1.619	52.6	973				12.97
	MR-AQCC/cc-pVQZ ⁱ		1.6175	52.76	995				12.87
	expt ^o		1.616						
$c^1 \Sigma_q^+ (c)^p$	CASSCF	49.185623	1.6503	36.57	928.5	10.95	1.60	6.60	22.23
5 (0)	MRCI	49.270498	1.6438	44.05	903.9	16.05	1.96	7.14	21.10
	MRCI+O	49.27466	1.648	44.2					20.9
	MRCI/[5s4p3d2f1g] ^c		1.653	44.6	868				20.95
	MR-AQCC/cc-pVQZ ⁱ		1.6545	44.75	829				20.89
	expt ^q		1.650						
$c^1 \Sigma_g^+(L)^p$	CASSCF	49.185270	1.9216	36.35	618.5	7.03	1.13	5.97	22.45
5.7	MRCI	49.262114	1.8716	38.79					26.36
	MRCI+Q	49.26645	1.8438	39.1					26.1

^{*a*} Internally contracted MRCI. ^{*b*} +Q refers to the multireference Davidson correction. ^{*c*} Ref 16a. ^{*d*} Ref 16b. ^{*e*} Ref 16c. ^{*f*} Ref 16e. ^{*h*} All electrons are correlated. ^{*i*} Ref 15a, D_0 value. ^{*k*} Ref 15b; thermochemical data, D_0 value. ^{*l*} Ref 15c. ^{*m*} Ref 15d. ^{*n*} Ref 15e; high-resolution Fourier transform emission spectroscopy. ^{*o*} Ref 15f; emission, UV and visible spectra of B₂. ^{*p*} Global (G) and local (L) minima. ^{*q*} Ref 15g; emission spectroscopy.

dissociation energies $D_e = 52$ kcal/mol at the MRCI level with respect to the adiabatic fragments Mg(³P) + B(²P); see Figure 1. With respect to the ground-state asymptotic fragments, either state is unbound by about 8.5 kcal/mol because of the significant Mg(³P \leftarrow ¹S) excitation energy of 2.603 eV (MRCI). B_2 . Table 3 lists our results on the first five states of B_2 ($X^3\Sigma_g^-$, $a^5\Sigma_u^-$, $A^3\Pi_u$, $b^1\Delta_g$, and $c^1\Sigma_g^+$), while corresponding PECs are plotted in Figure 2. Table 4 shows leading CASSCF configurations and Mulliken populations for these states. On the basis of the main CASSCF CFs and Mulliken popula-

tions, the bonding is adequately represented by the vbL diagrams 5-9.

 $X^{3}\Sigma_{g}^{-}$

 $a^{5}\Sigma_{u}$

 $A^{3}\Pi_{u}$

 $b^{1}\Delta_{g}$

 $B(^{2}P; M=\pm 1) \quad B(^{2}P; M=\mp 1)$

$$(\mathbf{B}) \rightarrow \mathbf{B} \rightarrow \mathbf{B}$$

 $B(^{2}P; M=0) \quad B(^{4}P; M=0)$

$$(\mathbf{B}) + \mathbf{i} = \mathbf{B} + \mathbf{B}$$

 $B(^{2}P; M=0) \quad B(^{2}P; M=\pm 1)$

 $B(^{2}P; M=\pm 1) B(^{2}P; M=\pm 1)$

B(²P; M=±1) B(²P; M=∓1)
$$c^{-1}\Sigma_{g}^{+}$$

The really fascinating bonding structures of $X^{3}\Sigma_{g}^{-}$, $a^{5}\Sigma_{u}^{-}$, $A^{3}\Pi_{u}$, $b^{1}\Delta_{g}$, and $c^{1}\Sigma_{g}^{+}$ consist of two $^{1}/_{2} \pi$, two $^{1}/_{2} \pi + ^{1}/_{2} \sigma$, one $^{1}/_{2} \sigma$ + one $^{1}/_{2} \pi$, one π (or two $^{1}/_{2} \pi$), and one π bond, respectively. Our numerical results shown in Table 3 are in very good agreement with previous theoretical values as well as with relevant experimental findings (experimental results on the $a^{5}\Sigma_{u}^{-}$ state do not seem to exist). Observe that the first four excited states span an energy range of about 25 kcal/mol; they are practically evenly spaced, while in the $c^{1}\Sigma_{g}^{+}$ state, an avoided crossing around 3.5 bohr gives rise to a local minimum at 3.54 bohr. In addition, with the exception of the $a^{5}\Sigma_{u}^{-}$ state which correlates to the first excited state of a single boron atom, $B(^{4}P) + B(^{2}P)$, the remaining four states trace their lineage to the ground-state B atoms; see Figure 2.

B. The Triatomic MgB₂. Table 5 collects total energies, equilibrium geometries (r_{Mg-B} , r_{B-B} , $\angle BMgB\equiv\varphi$), atomization energies (AE) with respect to the adiabatic fragments Mg + 2B, dipole moments (μ), Mulliken charges (q_{Mg} , q_B), and energy separations (T_e) of 36 states/isomers at the CASSCF, MRCI, and MRCI+Q levels of theory; for the ¹A₁ state only, MP2 and MP4 results are also reported. Figure 3 indicates relative energies of all MgB₂ states examined spanning an energy range of 4.2 eV; note that they are all bound with respect to the groundstate atoms Mg(¹S) + 2B(²P). In what follows, we describe in some detail the structure and bonding character of the first ten states in ascending energy order; the tenth state (\tilde{g}^5A_2) is located 32 kcal/mol above the \tilde{X}^1A_1 state.



Figure 2. Potential energy curves of the first five states of the B_2 molecule at the MRCI/cc-pVQZ level of theory. All energies have been shifted by +49 E_h .

 TABLE 4: Leading CASSCF Configuration Functions and Atomic Mulliken Distributions of the B2 Molecule

state	configuration ^a	2s	$2p_z$	$2\mathbf{p}_x$	$2p_y$
$\overline{X^{3}\Sigma_{g}^{-}}$	$ 1\sigma_{\rm g}^2[(0.89)1\sigma_{\rm u}^2 -$	1.41	0.55	0.50	0.50
	$(0.33)2\sigma_{\rm g}^2 [1\pi_{\rm ux}^{-1}1\pi_{\rm uy}^{-1}]$				
$a^5\Sigma_u^-$	$0.97 1\sigma_{g}^{2}1\sigma_{u}^{1}2\sigma_{g}^{1}1\pi_{ux}^{1}1\pi_{uy}^{1}\rangle$	1.24	0.74	0.50	0.50
$A^3\Pi_u$	$0.92/\sqrt{2} 1\sigma_{g}^{2}1\sigma_{u}^{2}2\sigma_{g}^{1}(1\pi_{ux}^{1}+i1\pi_{uy}^{1})\rangle$	1.63	0.77	0.29	0.29
$b^1\Delta_g$	$1/\sqrt{2}\{ 1\sigma_{g}^{2}[(0.87)1\sigma_{\mu}^{2}-$	1.39	0.57	0.50	0.50
	$(0.35)2\sigma_{g}^{2} 1\pi_{ux}^{1}1\bar{\pi}_{uy}^{1}\rangle +$				
	$0.62i 1\sigma_{g}^{2}1\sigma_{u}^{2}(1\pi_{ux}^{2}-1\pi_{uy}^{2})\rangle$				
$c^1 \Sigma_{g^+(G)}^{b}$	$0.61 1\sigma_{g}^{2}1\sigma_{u}^{2}(1\pi_{ux}^{2}+1\pi_{uy}^{2})\rangle$	1.40	0.54	0.52	0.52
$c^1 \Sigma_{g^+(L)}^{a^+(L)} b$	$0.91 1\sigma_{g}^{2}1\sigma_{u}^{2}2\sigma_{g}^{2}\rangle$	1.73	1.07	0.08	0.08

 a Only the σ valence electrons are enumerated. b Global (G) and local (L) minimum.

 $\tilde{X}^{I}A_{I}$ (*BMgB*). The main CASSCF equilibrium configurations of the $\tilde{X}^{1}A_{1}$ state, formally the ground state¹⁸ (vide infra), and corresponding Mulliken atomic populations (Mg/B + B) are

$$|\tilde{X}^{1}A_{1}\rangle \approx |1a_{1}^{2}2a_{1}^{2}1b_{1}^{2}[(0.87)1b_{2}^{2} - (0.26)3a_{1}^{2}]\rangle$$

$$3s^{0.96}3p_{z}^{0.08}3p_{x}^{0.23}3p_{y}^{0.13}/$$

$$(2s^{1.51}2p_{z}^{0.95}2p_{y}^{0.56})_{a}(2p_{x}^{1.69})_{b}(2s^{1.07}2p_{y}^{0.54}2p_{z}^{0.06})_{b}(2p_{x}^{0.08})_{a}$$

Note that only the eight valence electrons are counted. $(2s)_{a_1}$, $(2p_z)_{a_1}$, $(2p_x)_{b_1}$, and $(2p_y)_{b_2}$ refer to symmetric combinations and $(2p_y)_{a_1}$, $(2s)_{b_2}$, $(2p_z)_{b_2}$, and $(2p_x)_{a_2}$ to antisymmetric combinations of the relevant orbitals.

The formation of the BMgB \tilde{X}^1A_1 state can been thought of from either $B_2(X^3\Sigma_g^{-/3}B_1 \text{ in } C_{2\nu}) + Mg(^3P/^3B_1)$ or $MgB(^2\Pi$ -(4)) + B(^2P). Of course, the in situ Mg atom in the $^2\Pi(4)$ state of MgB is in its first excited $^3P(3s^13p^1)$ state; note that the $^2\Pi$ -(4) state of MgB is not included in Table 1. Both channels are

TABLE 5: Absolute Energies E (hartree), Bond Lengths r(Å) and Angles \angle BMgB $\equiv \varphi$ (deg), Atomization Energies AE (kcal/mol) with Respect to the Adiabatic Products, Dipole Moments μ (debye), Mulliken Charges on Mg and B (central B for the MgBB geometries) Atoms q, and Energy Separations T_e (kcal/mol) of the MgB₂, at Different Levels of Theory.

geometry	state	method ^{a,b}	-E	r _{Mg-B}	$r_{\rm B-B}$	φ	AE	$\langle \mu \rangle / \mu_{\mathrm{FF}}{}^c$	$q_{ m Mg}$	$-q_{\rm B}$	$T_{\rm e}$
Mg BB	$ ilde{X}^1 A_1$	CASSCF MRCI MRCI+Q MP2 MP4 RCCSD(T) RCCSD(T) ^d RCCSD(T) ^e	248.91786 249.02006 249.0259 248.98362 249.02142 249.02159 249.02191	2.245 2.225 2.225 2.243 2.251 2.223 2.224 2.224	$\begin{array}{c} 1.570 \\ 1.560 \\ 1.561 \\ 1.570 \\ 1.581 \\ 1.560 \\ 1.561 \\ 1.560 \end{array}$	40.93 41.06 41.1 40.96 41.10 41.08 41.10 41.1	93.4 108.1 109 115.9 113.8 107.9 107.9	4.66/4.66 5.00/4.99 /5.01 /5.14 /5.11	0.49 0.52	0.24 0.26	$\begin{array}{c} 0.0\\ 0.0\\ 0.0\\ 0.0\\ 0.0\\ 0.0\\ 0.0\\ 0.0$
Mg BB	ã ³ B ₁	CASSCF MRCI MRCI+Q RCCSD(T) RCCSD(T) ^d RCCSD(T) ^e	248.91411 249.01880 249.0254 249.01976 249.01988	2.300 2.279 2.279 2.272 2.274 2.274	1.625 1.617 1.617 1.616 1.616 1.616	41.37 41.55 41.5 41.67 41.63 41.6	91.1 107.3 109 106.7 106.6	4.23/4.23 4.71/4.75 /4.82 /4.99 /4.98	0.43 0.46	0.22 0.23	2.4 0.79 0.3 1.15 1.27 1.2
Mg-B-B	${ ilde b}^3\Sigma^-$	CASSCF MRCI MRCI+Q RCCSD(T) ^f RCCSD(T) ^d RCCSD(T) ^e	248.90897 249.00285 249.0085 249.00327 249.00298	2.287 2.266 2.265 2.270 2.268 2.263	1.578 1.578 1.581 1.574 1.573 1.556		87.8 97.3 98 96.4 96.0	2.76/2.76 3.02/3.12 /3.19 /2.88 /2.79	0.39 0.41	0.29 0.33	5.6 10.8 11 11.5 11.9 11.9
Mg-B-B	$\tilde{c}^5 \Sigma^-$	CASSCF MRCI MRCI+Q RCCSD(T) RCCSD(T) ^d RCCSD(T) ^e	248.90938 249.00112 249.0064 249.00313 249.00339	2.291 2.269 2.269 2.269 2.269 2.269 2.270	1.564 1.558 1.558 1.556 1.556 1.556		149.2 156.5 157 156.3 156.3	2.24/2.24 2.18/2.19 /2.18 /2.16 /2.17	0.39 0.40	0.29 0.33	5.3 11.9 12 11.6 11.6 11.8
Mg BB	\tilde{A}^1B_1	CASSCF MRCI MRCI+Q	248.89926 249.00001 249.0062	2.426 2.355 2.335	1.574 1.575 1.580	37.86 39.07 39.5	81.8 95.5 97	1.74/1.74 2.37/2.88 /3.11	0.39 0.40	0.20 0.20	11.7 12.6 12
Mg-B-B	$\tilde{B}^{1}\Delta$	CASSCF MRCI MRCI+Q	248.87383 248.97827 248.9855	2.283 2.257 2.256	1.610 1.607 1.610		65.8 81.9 84	2.53/2.53 3.11/3.27 /3.39	0.36 0.38	0.30 0.33	27.6 26.2 25
Mg B—B	\tilde{d}^3B_2	CASSCF MRCI MRCI+Q	248.87253 248.97416 248.9802	2.281 2.254 2.251	1.517 1.503 1.504	38.85 38.94 39.0	65.0 79.3 80	4.57/4.57 5.05/5.11 /5.16	0.48 0.50	0.24 0.25	28.4 28.8 29
Mg-B-B	ẽ³∏	CASSCF MRCI MRCI+Q	248.87170 248.97249 248.9789	2.132 2.105 2.105	1.517 1.519 1.519		64.5 78.3 79	7.38/7.38 7.45/7.40 /7.32	0.53 0.51	0.38 0.38	29.0 29.9 29
Mg BB	\tilde{f}^3A_1	CASSCF MRCI MRCI+Q	248.87277 248.97071 248.9770	2.554 2.535 2.538	1.680 1.672 1.675	38.39 38.51 38.5	65.1 77.2 78	1.00/1.00 1.30/1.38 /1.41	0.31 0.34	0.16 0.17	28.3 31.0 31
Mg BB	\tilde{g}^5A_2	CASSCF MRCI MRCI+Q	248.87381 248.96958 248.9751	2.539 2.511 2.512	1.519 1.504 1.504	34.80 34.86 34.9	126.9 136.7 137	1.57/1.57 1.68/1.67 /1.67	0.34 0.36	0.17 0.18	27.6 31.7 32
Mg-B-B	$10^{3}\Delta$	CASSCF MRCI MRCI+Q	248.86512 248.96709 248.9737	2.269 2.251 2.251	1.591 1.581 1.582		60.3 74.9 76	1.78/1.78 1.94/2.00 /2.03	0.38 0.40	0.32 0.35	33.1 33.2 33
Mg-B-B	$11^{1}\Sigma^{+}$	CASSCF MRCI MRCI+Q	248.86554 248.96579 248.9724	2.279 2.252 2.251	1.618 1.621 1.625		60.6 74.0 75	2.56/2.56 3.18/3.35 /3.49	0.35 0.37	0.29 0.32	32.8 34.1 34
Mg BB	12 ⁵ B ₁	CASSCF MRCI MRCI+Q	248.86714 248.96575 248.9719	2.410 2.401 2.404	1.652 1.644 1.643	40.09 40.03 40.0	122.7 134.3 135	2.07/2.07 2.09/2.09 /2.10	0.50 0.48	0.25 0.24	31.8 34.1 34
Mg BB	13 ³ A ₂	CASSCF MRCI MRCI+Q	248.86780 248.96462 248.9702	2.444 2.413 2.413	1.515 1.504 1.504	36.11 36.31 36.3	62.0 73.3 74	2.42/2.42 2.66/2.81 /2.87	0.42 0.42	0.21 0.21	31.4 34.8 35
Mg-B-B	$14^{1}\Sigma^{-}$	CASSCF MRCI MRCI+Q	248.85741 248.95868 248.9653	2.238 2.241 2.244	1.577 1.574 1.576		55.5 69.6 71	1.85/1.85 1.87/1.92 /1.90	0.44 0.42	$\begin{array}{c} 0.41 \\ 0.40 \end{array}$	37.9 38.5 38
Mg-B-B	15 ¹ Π	CASSCF MRCI MRCI+Q	248.85659 248.95655 248.9633	2.183 2.134 2.128	1.528 1.526 1.528		55.0 68.2 70	4.93/4.93 5.40/5.76 /5.87	0.57 0.53	0.46 0.42	38.5 39.9 39
Mg-B-B	$16^{3}\Sigma^{+}$	CASSCF MRCI MRCI+Q	248.85625 248.95376 248.9597	2.263 2.245 2.245	1.599 1.596 1.598		54.8 66.5 67	1.71/1.71 1.88/1.94 /1.97	0.37 0.39	0.32 0.35	38.7 41.6 42

TABLE 5: Continued.

	commutat										
geometry	state	method ^{a,b}	-E	r _{Mg-B}	$r_{\rm B-B}$	φ	AE	$\langle \mu \rangle / \mu_{\rm FF}^c$	$q_{ m Mg}$	$-q_{\rm B}$	T _e
Mg BB	17 ¹ A ₂	CASSCF MRCI MRCI+Q	248.82611 248.93301 248.9404	2.395 2.362 2.357	1.551 1.588 1.596	37.78 39.29 39.6	35.9 53.5 55	2.70/2.70 3.02/3.15 /3.19	0.41 0.38	0.20 0.19	57.6 54.6 54
Mg BB	18 ⁵ B ₂	CASSCF MRCI MRCI+Q	248.83253 248.92674 248.9321	2.370 2.366 2.369	1.514 1.504 1.503	37.26 37.08 37.0	101.0 109.8 110	2.22/2.22 2.24/2.24 /2.23	0.51 0.50	0.26 0.25	53.5 58.6 59
Mg BB	$19^1B_2 \; {}_{global}$	CASSCF MRCI MRCI+Q	248.82542 248.92670 248.9329	2.381 2.366 2.366	1.458 1.450 1.450	35.64 35.68 35.7	35.4 49.5 51	1.83/1.83 1.80/1.81 /1.83	0.45 0.41	0.22 0.21	58.0 58.6 58
	$19^{1}B_{2 \ local}$	CASSCF MRCI MRCI+Q	248.78913 248.89158 248.8993	2.449 2.433 2.435	2.381 2.179 2.147	58.16 53.22 52.3	12.7 27.5 29	3.01/3.01 3.70/3.73 /3.74	0.42 0.42	0.21 0.21	80.8 80.6 79
Mg-B-B	20 ⁵ ∏	CASSCF MRCI MRCI+Q	248.81307 248.90048 248.9056	2.303 2.299 2.302	1.503 1.501 1.502		88.8 93.3 93	5.00/5.00 4.77/4.76 /4.65	0.61 0.58	0.49 0.49	65.8 75.0 76
B-Mg-B	$21^{1}\Delta_{g}$	CASSCF MRCI MRCI+Q	248.79209 248.90040 248.9090	2.317 2.281 2.279			14.5 33.0 36		0.53 0.62	0.27 0.31	78.9 75.1 73
B-Mg-B	$22^{3}\Sigma_{g}^{-}$	CASSCF MRCI MRCI+Q	248.79288 248.90011 248.9085	2.311 2.274 2.273			15.0 32.9 35		0.49 0.59	0.25 0.30	78.4 75.3 74
B-Mg-B	$23^{1}\Sigma_{g}^{+}$	CASSCF MRCI MRCI+Q	248.79112 248.89949 248.9080	2.320 2.285 2.283			13.9 32.4 35		0.54 0.63	0.27 0.31	79.5 75.7 74
B-Mg-B	$24^{1}\Sigma_{u}{}^{-}$	CASSCF MRCI MRCI+Q	248.79047 248.89888 248.9074	2.322 2.287 2.286			13.5 32.1 35		0.54 0.64	0.27 0.32	79.9 76.0 74
B-Mg-B	$25^{3}\Pi_{u}$	CASSCF MRCI MRCI+Q	248.78964 248.89687 248.9055	2.445 2.394 2.391			13.0 30.8 33		0.41 0.50	0.21 0.25	80.5 77.3 76
B-Mg-B	$26^3\Delta_u$	CASSCF MRCI MRCI+Q	248.78807 248.89662 248.9052	2.315 2.282 2.281			12.0 30.7 33		0.57 0.65	0.28 0.33	81.5 77.5 76
B-Mg-B	$27^{3}\Sigma_{u}{}^{+}$	CASSCF MRCI MRCI+Q	248.78748 248.89604 248.9046	2.318 2.285 2.284			11.6 30.3 33		0.57 0.66	0.29 0.33	81.8 77.8 76
B-Mg-B	$28^5\Sigma_u^{-}$	CASSCF MRCI MRCI+Q	248.78804 248.89446 248.9027	2.271 2.245 2.245			73.1 89.6 93		0.52 0.62	0.26 0.31	81.5 78.8 77
B-Mg-B	$29^{5}\Delta_{g}$	CASSCF MRCI MRCI+Q	248.78161 248.88957 248.8980	2.287 2.260 2.259			69.0 86.5 89		0.61 0.69	0.30 0.35	85.5 81.9 80
B-Mg-B	$30^5\Sigma_g^+$	CASSCF MRCI MRCI+Q	248.78110 248.88907 248.8975	2.288 2.261 2.260			68.7 86.2 88		0.61 0.70	0.31 0.35	85.8 82.2 81
Mg-B-B	31 ⁵ Δ	CASSCF MRCI MRCI+Q	248.78881 248.88882 248.8954	2.275 2.251 2.250	1.798 1.794 1.797		73.6 86.0 87	-0.14/-0.14 0.62/0.76 /0.87	0.21 0.26	0.17 0.21	81.0 82.4 82
Mg-B-B	$32^5\Sigma^+$	CASSCF MRCI MRCI+Q	248.78620 248.88597 248.8925	2.276 2.251 2.250	1.801 1.799 1.801		71.9 84.2 85	-0.22/-0.22 0.56/0.71 /0.82	0.20 0.25	0.16 0.20	82.6 84.2 84
B-Mg-B	$33^{1}\Pi_{g}$	CASSCF MRCI MRCI+Q	248.76773 248.87498 248.8841	2.553 2.446 2.434			0.8 17.1 20		0.22 0.37	0.11 0.19	94.2 91.0 89
Mg BB	34 ⁵ A ₁	CASSCF MRCI MRCI+Q	248.77367 248.86926 248.8754	2.385 2.303 2.297	1.734 1.696 1.692	42.63 43.21 43.22	64.1 73.7 74	4.34/4.34 5.01/5.32 /5.43	0.57 0.59	0.28 0.29	90.5 94.6 94
B-Mg-B	$35^5\Pi_g$	CASSCF MRCI MRCI+Q	248.75807 248.86616 248.8747	2.224 2.194 2.193			54.3 71.8 74		0.55 0.65	0.28 0.32	100.3 96.6 95

^{*a*} Internally contracted MRCI. ^{*b*} +Q refers to the multireference Davidson correction. ^{*c*} $\langle \mu \rangle$ calculated as expectation value; μ_{FF} calculated by the finite field method. ^{*d*} RCCSD(T) based on CASSCF orbitals. ^{*e*} Ref 9, RCCSD(T)/aug-cc-pVQZ level of theory. ^{*f*} RCCSD(T) based on five configuration CASSCF orbitals.



Figure 3. Relative energy levels of MgB_2 at the MRCI/cc-pVQZ level.

consistent with the following vbL bonding representation of the BMgB \tilde{X}^1A_1 (=³B₁ \otimes ³B₁) state.



The bonding comprises one " σ "-like (in-plane) and one " π "-like (out-of-plane) 2e⁻⁻³ center bonds represented by the two isosceles triangles shown in diagram 10. The vbL diagram (10) is in accordance with the Mulliken distributions given above: About 0.7 e⁻ are transferred from the metal to the in situ B₂ moiety through the " π " plane, while about 0.2 e⁻ are moving back from B₂ to Mg through the " σ " plane. The BB bond length in the \tilde{X}^1A_1 state decreases considerably as compared to the free B₂ ($X^3\Sigma_g^-$) at the same level of theory, $\Delta r = -0.04$ Å (see Tables 3 and 5). Therefore, it is clear that the two B atoms can be considered bonded in the \tilde{X}^1A_1 state of MgB₂.

At infinity, the wave function can be described by the product $|{}^{1}S\rangle_{Mg} \times |{}^{2}P\rangle_{B} \times |{}^{2}P\rangle_{B}$ and the atomization energy with respect to the ground-state atoms (see Figure 4) is 108.1(109) kcal/mol at the MRCI(+Q) level of theory, Table 5. Correcting with respect to the zero-point harmonic vibrational (ZPE) energy, $\omega_{1}(B_{2}) = 453.6$, $\omega_{2}(A_{1}) = 494.7$, and $\omega_{3}(A_{1}) = 1079.6$ cm⁻¹ as obtained at the MP2 level, the atomization energy becomes $108.1(109) - {}^{1}/{}_{2}(\omega_{1} + \omega_{2} + \omega_{3}) = 105.2(106)$ kcal/mol. With respect to the adiabatic products $B_{2}(b^{1}\Delta_{g}) + Mg({}^{1}S)$ (see Figure 4 and diagram 8) the MRCI(+Q) dissociation energy is $D_{e} = 55.6(56)$ kcal/mol, or $D_{0} = D_{e} - ZPE(BMgB) + \omega_{e}/2[B_{2}(b^{1}\Delta g)] = 55.6(56) - 2.90 + 1.42 = 54.1(55)$ kcal/mol.



Figure 4. MRCI potential energy profiles of the \tilde{X}^1A_1 and \tilde{a}^3B_1 states of MgB₂ molecule, keeping the B–B distance or the angle φ at their equilibrium values. All energies have been shifted by +248 $E_{\rm h}$.

Moving from $C_{2\nu}$ [BMgB(\tilde{X}^1A_1)] symmetry to the linear $D_{\infty h}$ structure, or $\tilde{X}^1A_1 \rightarrow {}^1\Delta_g$, the MRCI(+Q) barrier to linearity is 75.1(73) kcal/mol, Figure 5. The ${}^1\Delta_g$ state is the lowest of BMgB linear geometry giving rise to two Renner–Teller components, \tilde{X}^1A_1 and \tilde{A}^1B_1 , upon bending. The bonding vbL diagram of the ${}^1\Delta_g$ structure is shown below.

$$y_{r} \xrightarrow{X} z_{2s} \xrightarrow{Y} z_{3s} \xrightarrow{Y} z_{3s$$

B(²P; M=0) Mg(³P; M=±1) B(²P; M=±1)
$$21^{1}\Delta_{g}(1)$$

The CASSCF Mulliken atomic populations (Mg/B) $3s^{0.82}3p_z^{0.32}3p_x^{0.12}3p_y^{0.12}/2s^{1.67}2p_z^{0.68} 2p_x^{0.45}2p_y^{0.45}$ are in conformity with diagram 11. Table 5 lists numerical results concerning the ${}^{1}\Delta_{g}$ (transition) linear state.

 $\tilde{a}^{3}B_{1}$ (*BMgB*). The leading equilibrium CASSCF configurations and atomic Mulliken populations of the $\tilde{a}^{3}B_{1}$ state, formally the first excited state of MgB₂¹⁸ located 0.79(0.3)[1.15] kcal/ mol above the $\tilde{X}^{1}A_{1}$ state at the MRCI(+Q)[CCSD(T)] level, are as follows (Mg/B+B):

$$|{}^{3}B_{1}\rangle = \sim |[0.89(1a_{1}{}^{2}2a_{1}{}^{2}3a_{1}{}^{1}) - 0.17(1a_{1}{}^{2}3a_{1}{}^{1}4a_{1}{}^{2})]1b_{1}{}^{1}1b_{2}{}^{2}\rangle$$

$$3s^{1.10}3p_{z}^{0.11}3p_{x}^{0.07}3p_{y}^{0.19}/ (2s^{1.68}2p_{z}^{1.00}2p_{y}^{1.02})(2p_{x}^{0.86})(2s^{1.14}2p_{y}^{0.51}2p_{z}^{0.08})(2p_{x}^{0.05})$$

Figure 4 shows the potential energy profile with respect to Mg + B₂; the bond distance of B₂ is fixed to the equilibrium value of the $\tilde{a}^{3}B_{1}$ state along the potential curve but is relaxed to the



Figure 5. MRCI potential energy profiles of the \tilde{X}^1A_1 , \tilde{a}^3B_1 , and \tilde{A}^1B_1 states of MgB₂ with respect to the angle φ , while keeping the r_{Mg-B} distance at its equilibrium value. Energies shifted by +248 $E_{\rm h}$.

 $X^{3}\Sigma_{g}^{-}$ bond length at infinity. The bonding can be described by the vbL icon (12).



The in situ B₂ finds itself in the A³Π_u (³B₁) state with the Mg in its ground ¹S state; however, as seen in Figure 4, it correlates to B₂(X³Σ_g⁻) + Mg(¹S). The bonding is due to a transfer of about 0.7 e⁻ from the 3s²(2a₁²) pair of Mg to the empty 2p_z orbitals of B atoms ("in-plane", σ character), with a concomitant back transfer of 0.1 and 0.2 e⁻ from the 2p_x¹(b₁) single electron and ~2s²(b₂) pair of the B₂ moiety to the 3p_x and 3p_y empty orbitals of Mg, respectively; see diagram 12. Thus, a net charge of about 0.4 e⁻ is moving from Mg to B₂. With respect to B₂(X³Σ_g⁻) + Mg(¹S), the MRCI(+Q) binding energy is 41.7(43) kcal/mol. The MRCI B–B bond distance and ∠BMgB angle increase by 0.06 Å and 0.5 deg as compared to the \tilde{X}^1A_1 state.

Figure 5 shows the potential energy profile of the \tilde{a}^3B_1 state with respect to the $\angle BMgB$ angle. The corresponding linear structure BMgB of ${}^3\Sigma_g{}^-$ symmetry is (accidentally) degenerate to the ${}^1\Delta_g$ structure, which correlates to \tilde{X}^1A_1 (vide supra), with a barrier to linearity of 74.5 kcal/mol. The population analysis (Mg/B) $3s^{0.23}3p_z^{0.29}3p_x^{0.16}3p_y^{0.16}2s^{1.68}2p_z^{0.68}2p_x^{0.44}2p_y^{0.44}$ supports the vbL icon (13).

 $\tilde{b}^{3}\Sigma^{-}$ (*MgBB*). This is the second excited state of MgB₂ or the ground state of the linear MgBB isomer, located 11 kcal/ mol above the (formal) ground state $\tilde{X}^{1}A_{1}$. The formation of

 $B(^{2}P; M=\pm 1) Mg(^{1}S) B(^{2}P; M=\mp 1) 22^{3}\Sigma_{g}(1)$

the molecule can be thought of as either MgB(X²Π) + B(²P) or Mg(¹S) + B₂(X³Σ_g⁻); the corresponding potential energy profiles are displayed in Figure 6. At the MRCI(+Q) level, the dissociation energies with respect to MgB + B or Mg + B₂ are 84.5(85) and 31.7(33) kcal/mol, respectively.

This is a truly multireference state as is evidenced from the leading CASSCF configurations

$$\tilde{b}^{3}\Sigma^{-}\rangle \approx |[0.69(1\sigma^{2}2\sigma^{2}3\sigma^{2}) - 0.47(1\sigma^{2}2\sigma^{2}4\sigma^{2})]1\pi_{x}^{-1}1\pi_{y}^{-1} + (1\sigma^{2}2\sigma^{2}3\sigma^{1}4\sigma^{1})[0.37(1\bar{\pi}_{x}^{-1}1\pi_{y}^{-1}) + 0.26(1\pi_{x}^{-1}1\bar{\pi}_{y}^{-1})]\rangle$$

With the help of the Mulliken CASSCF atomic populations

$$3s^{1.03}3p_z^{0.51}3p_x^{0.01}3p_y^{0.01}/2s^{1.33}2p_z^{0.93}2p_x^{0.49}2p_y^{0.49}/2s^{1.36}2p_z^{0.71}2p_x^{0.50}2p_y^{0.50}$$

the bonding can be captured by the vbL graph (14).

$$C = Mg - B = Mg - B = (14)$$

Mg(¹S) B(²P; M=±1) B(²P; M=±1) \tilde{b} ³ Σ (1)

A total of 0.4 e⁻ are transferred from Mg to B₂ along the σ frame, about 0.3 e⁻ to the central B atom and 0.1 e⁻ to the second B directly linked to the central B atom.

The MRCI(+Q)[RCCSD(T)] atomization energy with respect to Mg(¹S) + 2B(²P) is 97.3(98)[96.4] kcal/mol. Perhaps it should be mentioned at this point that the RCCSD(T) calculations were based on CASSCF orbitals. Finally, the bond distances r_{Mg-B} and r_{B-B} are shorter by 0.12 and 0.02 Å as compared to the free MgB(X²\Pi) and B₂(X³Σ_g⁻), respectively.

 $\tilde{c}^5\Sigma^-$ (*MgBB*). This linear high-spin excited state is located 12 kcal/mol above the \tilde{X}^1A_1 state and just 1 kcal/mol higher than the $\tilde{b}^3\Sigma^-$ state at the MRCI or MRCI+Q level. However, at the RCCSD(T) level of theory, the $\tilde{b}^3\Sigma^-$ and $\tilde{c}^5\Sigma^-$ states are degenerate; therefore, the labeling of the ${}^5\Sigma^-$ state as "c" is only formal. Similar results are reported in ref 8. As expected, this state has a single reference character, $|c^5\Sigma^-\rangle =$ $\sim 0.96|1\sigma^2 2\sigma^2 3\sigma^1 4\sigma^1 1\pi_x^{-1} 1\pi_y^{-1}\rangle$, which in conjunction with the Mulliken atomic populations (Mg/B/B)

$$3s^{1.01}3p_z^{0.54}3p_x^{0.01}3p_y^{0.01}/2s^{1.30}2p_z^{0.98}2p_x^{0.48}2p_y^{0.48}/2s^{1.32}2p_z^{0.72}2p_x^{0.51}2p_y^{0.51}$$

points to the following vbL bonding diagram:

Mg(³P; M=0) B(²P; M=±1) B(²P; M=±1) $\widetilde{c}^{5}\Sigma(1)$

Note that, similarly to the $\tilde{b}^3 \Sigma^-$ state, the in situ B₂ moiety is in the ${}^3\Sigma_g{}^-$ state, but the in situ Mg atom is excited to the ${}^3P(3s^{1}-3p^{1})$ term. Nevertheless, by pulling apart the Mg atom, i.e., Mg + B₂, the $\tilde{c}^5\Sigma^-$ correlates to the first excited state of B₂($a^5\Sigma^-$) + Mg(1S); see Figure 6. Imagining this state as formed from MgB + B, i.e., by pulling away the terminal B atom, the $\tilde{c}^5\Sigma^-$



Figure 6. MRCI potential energy profiles of the $\tilde{b}^3\Sigma^-$ and $\tilde{c}^5\Sigma^-$ states of MgB₂ keeping the B–B or the Mg–B distances at their equilibrium values. Energies shifted by +248 $E_{\rm h}$.

state correlates to the $b^4\Pi$ state of MgB (diagram 4) + B(²P; M = ±1); see Figure 6.

With respect to the first channel, $Mg({}^{1}S) + B_{2}(a^{5}\Sigma^{-})$, the adiabatic binding energy is $D_{e} = 35.2(37)$ kcal/mol; diabatically, namely, $Mg({}^{3}P) + B_{2}(X^{3}\Sigma^{-})$, $D_{e} = 90.7(92)$ kcal/mol at the MRCI(+Q) level. With respect to the second channel, MgB-(b⁴\Pi) + B({}^{2}P), $D_{e} = 103.3(104)$ kcal/mol.

 $\tilde{A}^{1}B_{1}$ (*BMgB*). Formally, this is the fourth excited state and the third of C_{2v} symmetry, lying 12.6(12) kcal/mol higher than the $\tilde{X}^{1}A_{1}$ state. Its energy distance from the $\tilde{c}^{5}\Sigma^{-}$ is just 0.7 kcal/mol but by adding the Davidson correction these two states become degenerate; see Table 5 and Figure 3.

The most important CASSCF configurations and corresponding Mulliken atomic densities (Mg/B + B) are as follows:

$$|\tilde{A}^{1}B_{1}\rangle = \sim |1a_{1}^{2}2a_{1}^{2}3a_{1}^{1}[(0.88)1\bar{b}_{1}^{-1}1b_{2}^{-2} - (0.27)4a_{1}^{-2}1\bar{b}_{1}^{-1}]\rangle$$

$$\frac{3s^{1.05}3p_z^{0.40}3p_x^{0.05}3p_y^{0.07}}{(2s^{1.59}2p_z^{1.43}2p_y^{0.58})(2p_x^{0.88})(2s^{1.14}2p_y^{0.51}2p_z^{0.10})(2p_x^{0.05})}$$

As in the case of the \tilde{X}^1A_1 , the wave function of the \tilde{A}^1B_1 state at infinity can be described by the product $|Mg(^1S)\rangle \times$ $|B(^2P)\rangle \times |B(^2P)\rangle$, but the in situ Mg atom is in its first excited state, $^{3}P(3s^{1}3p^{1})$. The molecule can be thought of either as Mg- $(^{3}P) + B_2(X^{3}\Sigma_g^{-})$ or as MgB + B(²P). The bonding is graphically shown in diagram 16. A total of about 0.4 e⁻ are



transferred from Mg to B₂: 0.6 e⁻ are moving from Mg to B through the $\sigma(a_1)$ plane (2 e⁻ - 3 centers), while about 0.2 e⁻ are back-transferred through the π (1 e⁻ - 3 centers) plane and $\sigma(b_2)$ bond.

The MRCI(+Q) atomization energy with respect to Mg(1 S) + 2B(2 P) is 95.5(97) kcal/mol. In comparison with the ground state, the Mg-B distance increases by 0.13 Å, while the B-B one increases only slightly.

 $\tilde{B}^{1}\Delta(MgBB)$, $\tilde{e}^{3}\Pi(MgBB)$. The fifth and seventh excited states have linear geometry; they are of symmetries ${}^{1}\Delta$ and ${}^{3}\Pi$ and are located 26 and 30 kcal/mol above the ground state, respectively (Figure 3). Their leading CASSCF equilibrium configurations and atomic Mulliken population are (Mg/B/B)

$$\begin{split} |\tilde{B}^{1}\Delta_{1}\rangle &= \sim |[0.56(1\sigma^{2}2\sigma^{2}3\sigma^{2}) - \\ & 0.35(1\sigma^{2}2\sigma^{2}4\sigma^{2})](1\pi_{x}^{2} - 1\pi_{y}^{2})\rangle \\ 3s^{1.13}3p_{z}^{0.42}3p_{x}^{0.02}3p_{y}^{0.02}/2s^{1.35}2p_{z}^{0.86}2p_{x}^{0.52}2p_{y}^{0.52}/ \\ & 2s^{1.37}2p_{z}^{0.73}2p_{x}^{0.46}2p_{y}^{0.46} \\ |\tilde{e}^{3}\Pi_{1}\rangle &= \sim 1/\sqrt{2}|[0.90(1\sigma^{2}2\sigma^{2}3\sigma^{1}) - \\ & 0.19(1\sigma^{2}3\sigma^{1}4\sigma^{2})](1\pi_{x}^{-1}1\pi_{y}^{-2} + 1\pi_{x}^{-2}1\pi_{y}^{-1})\rangle \\ 3s^{1.11}3p^{0.07}3p^{0.07}3p^{0.16}/2s^{1.18}2p^{0.64}2p^{0.51}2p^{1.02}/2s^{1.02}/2s^{1.02}/2s^{1.02}/2s^{1.02}/2s^{1.02}/2s^{0.02$$

$$2s^{1.24}2p_z^{0.67}2p_x^{0.41}2p_y^{0.78}$$

The bonding character of both states is captured by the vbL diagrams 17 and 18.

$$\mathbf{G} = \mathbf{M} \mathbf{g} - \mathbf{B} - \mathbf{B} \mathbf{H} \mathbf{g}$$

Mg(¹S) B(²P; M=±1) B(²P; M=±1) $\tilde{B}^{1}\Delta(1)$

$$Mg^{\prime}S) \quad B^{\prime}P: M=0) \quad B^{\prime}P: M=\pm 1) \qquad \tilde{e}^{3}\Pi(1) \qquad (18)$$

From diagram 17, it is obvious that in the $\tilde{B}^1\Delta$ state its "natural constituents" are Mg(¹S) + B₂(b¹\Delta_g; Scheme 8). One π bond (B–B) and two σ bonds tie the molecule together, giving rise to an atomization energy of 81.9(84) kcal/mol at the MRCI-(+Q) level. Note that the B–B bond distance [1.607(1.610) Å] in the $\tilde{B}^1\Delta$ state is practically the same as the bond distance of the free B₂ in the b¹\Delta_g state [1.617(1.618) Å], as the vbL diagram (17) suggests.

In the $\tilde{e}^3\Pi$ state, the central in situ B atom is in its first excited ${}^{4}P(2s^{1}2p^{2})$ state; therefore, the in situ B₂ molecule is in the ${}^{3}\Pi_{g}$ -(2) state (not included in Table 3). From vbL diagrams 17 and 18, it is suggested that the Mg–B and B–B bond lengths in the $\tilde{e}^{3}\Pi$ state should be shorter than the corresponding ones in the $\tilde{B}^{1}\Delta$ state. The Mg–B σ bond in the $\tilde{e}^{3}\Pi$ state should decrease, because the Mg(¹S) atom faces a more "exposed" B(⁴P) atom, and this is indeed what is observed: The Mg–B and B–B bond lengths are shorter by 0.15 and 0.09 Å in the $\tilde{e}^{3}\Pi$ state as compared to the $\tilde{B}^{1}\Delta$ state. These differences are in agreement with the observed ones in the appropriate states of the free MgB [${}^{4}\Sigma^{-}(3)$, X²\Pi] and B₂ [${}^{3}\Pi_u(2)$, b¹ Δ_g] molecules. Finally, the atomization energy of the $\tilde{e}^{3}\Pi$ state with respect to the ground-state atoms Mg(¹S) + 2B(²P) (asymptotic products) is 78.3(79) kcal/mol.

Electronic and Geometric Structure of MgB2

 $\tilde{d}^3B_2(BMgB)$, $\tilde{f}^3A_1(BMgB)$, and $\tilde{g}^5A_2(BMgB)$. These are the last discussed states in the present work; they are of V-shaped geometry located 29, 31, and 32 kcal/mol above the \tilde{X}^1A_1 state (Table 5, Figure 3). Their leading equilibrium CASSCF CFs, Mulliken populations, and bonding vbL graphical representations follow:

$$|\tilde{d}^{3}B_{2}\rangle = \sim |[0.88(1a_{1}^{2}2a_{1}^{2}3a_{1}^{1}) + 0.22(1a_{1}^{2}3a_{1}^{1}4a_{1}^{2})]1b_{1}^{2}1b_{2}^{1}\rangle$$

$$\frac{3s^{1.02}3p_z^{0.11}3p_x^{0.24}3p_y^{0.05}}{(2s^{1.68}2p_z^{0.92}2p_y^{1.09})(2p_x^{1.39})}{(2s^{0.64}2p_y^{0.34}2p_z^{0.05})(2p_x^{0.08})}$$

$$Mg^{(S)} = B B B$$

$$B^{2}P B^{(P)} B^{(P)} d^{3}B_{2}$$

$$Mg^{(S)} = B B B$$

$$Mg^{(19)} = B^{(19)} B^{(19)} = B^{(19)} = B^{(19)} B^{(19)} = B^{$$

$$|f^{3}A_{1}\rangle = \sim 0.92|1a_{1}^{2}2a_{1}^{2}3a_{1}^{4}4a_{1}^{4}1b_{2}^{2}\rangle$$

$$3^{s_{110}} 3^{p_z^{0.43}} 3^{p_z^{0.00}} 3^{p_y^{0.00}} / (2^{s_{1.75}} 2^{p_z^{1.55}} 2^{p_y^{1.16}}) (2^{p_x^{0.06}}) (2^{s_{1.27}} 2^{p_y^{0.46}} 2^{p_z^{0.10}}) (2^{p_z^{0.04}})$$

$$\begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & &$$

$$\tilde{g}^{5}A_{2}\rangle = \sim 0.92|1a_{1}^{2}2a_{1}^{2}3a_{1}^{1}4a_{1}^{1}1b_{1}^{1}1b_{2}^{1}\rangle$$

 $3s^{1.16}3p_z^{0.40}3p_x^{0.03}3p_y^{0.03}/(2s^{1.73}2p_z^{1.36}2p_y^{1.14})(2p_x^{0.92})$ $(2s^{0.68}2p_y^{0.33}2p_z^{0.07})(2p_x^{0.03})$



Diagrams 19 and 21 show that the two in situ B atoms are nonequivalent, one in the ground (²P) and the other in its first excited ⁴P state. But obviously, they should be equivalent on account of symmetry; the mirror images with respect to a symmetry plane bisecting the BMgB angle ensure the $C_{2\nu}$ symmetry invariance. Note also that, in the \tilde{g}^5A_2 state, two of the in situ atoms, the (unique) Mg and "one" of B atoms are excited.

Approximately 0.5, 0.3, and 0.3 e⁻ are transferred from the Mg atom to the B₂ moiety in the \tilde{d}^3B_2 , \tilde{f}^3A_1 , and \tilde{g}^5A_2 states, respectively. It is interesting that the B–B distance in the \tilde{d}^3B_2 and \tilde{g}^5A_2 states is the smallest of all the MgB₂ states presently studied, about 0.1 Å shorter than the free B₂(X³\Sigma_g⁻). Finally, the adiabatic MRCI(+Q) atomization energies with respect to



Figure 7. Projection of the crystal structure of MgB₂ looking from above and along the *c* axis (*P/mmm*), $\bullet - \bullet$ (Mg-Mg) = 3.08 Å, $\bigcirc - \bigcirc$ (B-B) = 1.78 Å, $\bullet - \bigcirc$ (Mg-B) = 2.50 Å, \angle BMgB $\equiv \varphi = 41.6^{\circ}$.

 $Mg(^{1}S) + 2B(^{2}P)[\tilde{d}^{3}B_{2}, \tilde{f}^{3}A_{1}]$ and $Mg(^{3}P) + 2B(^{2}P)[\tilde{g}^{5}A_{2}]$, are 79.3 (80), 77.2 (78), and 136.7 (137) kcal/mol, respectively.

Numerical results for the remaining 24 states presently investigated are listed in Table 5, 6 of which are V-shaped, 8 linear of the MgBB type, and 10 linear of centrosymmetric configuration, B-Mg-B. Two of the centrosymmetric structures previously described, ${}^{1}\Delta_{g}$ and ${}^{3}\Sigma_{g}^{-}$, are transition states, but we did not try to calculate frequencies for the remaining 10 B-Mg-B states.

4. Summary and Remarks

Motivated by the recently discovered high superconducting transition temperature $T_c = 39$ K of crystalline MgB₂, we have examined by all-electron ab initio multireference and coupledcluster methods the isolated MgB₂. A total of 36 states (including some transition states) were calculated spanning an energy range of 4.2 eV, all of which are bound with respect to the ground-state atoms, Mg(¹S) + 2B(²P). In addition, we have calculated full potential energy curves for 17 states of the diatomic MgB. As far as we know, only 2 theoretical studies exist in the literature on MgB,^{13,14} while experimental results are completely lacking.

Focusing on the triatomic MgB₂, our most import findings can be summarized as follows.

(a) Although formally the ground state is of ${}^{1}A_{1}$ symmetry, a strong contender is a ${}^{3}B_{1}$ state differing in energy by less than 1 kcal/mol, $T_{e} = 0.79(0.3)$ kcal/mol at the MRCI(+Q) level. In other words, the ${}^{1}A_{1}$ and ${}^{3}B_{1}$ states are degenerate within the accuracy of our calculations.

(b) In all states, about 0.2 to 0.6 electrons are moving from the Mg atom to the in situ B_2 moiety.

(c) The next V-shaped state (\tilde{A}^1B_1) is located 12 kcal/mol above the \tilde{X}^1A_1 , while two more $C_{2\nu}$ states $(\tilde{d}^3B_2, \tilde{f}^5A_2)$ are well-separated from the ground state, located about 30 kcal/ mol higher.

(d) The bonding in most of the MgB_2 states studied here, but in particular the V-shaped ones, is quite unconventional because of the extraordinary bonding agility of the B atom and the ensuing unusual distribution of the active electrons on the B_2 molecule.

(e) Schematically, the spatial arrangement of the atoms of crystalline MgB₂ (space group *P6/mmm*) is shown in the projection in Figure 7, looking down and along the (unique) *c* crystallographic axis. The top plane is formed of Mg (\bullet) atoms, and the plane underneath of B atoms (\bigcirc). The three atoms of the MgB₂ units are in special crystallographic positions, namely

(0, 0, 0), $(\frac{1}{3}, \frac{2}{3}, \frac{1}{2})$, and $(\frac{2}{3}, \frac{1}{3}, \frac{1}{2})$ corresponding to Mg, B, and B atoms, respectively (see also ref 3).

From Figure 7, we observe that the solid structure is composed of identical isosceles triangles; therefore, relevant states of a single (isolated) MgB₂ molecule (and excluding higher states) can only be the two practically degenerate \tilde{X}^1A_1 and \tilde{a}^3B_1 states.

Mg–B and B–B distances are larger in the crystal structure as compared to the isolated molecule by about 0.25 and 0.20 Å, respectively. Remarkably, however, the \angle BMgB (= φ) angle is identical in the solid state ($\varphi = 41.6^{\circ}$) and in the $\tilde{X}^{1}A_{1}(\varphi =$ 41.1°) or $\tilde{a}^{3}B_{1}(\varphi = 41.6^{\circ})$ molecular state.

(f) Our calculations indicate that electrons are fed copiously from the Mg layers to the B layers. We dare suggest that in the crystalline environment each Mg atom can lose up to one electron or more, transferred to two equivalent B atoms. Our bonding analysis of the \tilde{X}^1A_1 and \tilde{a}^3B_1 states points to σ (inplane) and π (out-of-plane) bands in the solid phase. In the latter, the superconductivity is allowed by both perpendicular (π bands) and parallel (σ bands) bands to the boron sheets.²

Obviously, the connection of an isolated species (here, MgB_2) to the relevant polymeric crystal (here, $(MgB_2)_x$) is far from trivial. We hope however that the present study and analysis can be of some help for the better understanding of this very interesting material.

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(18) Our preliminary calculations using the cc-pVDZ basis reverse the order of the two lowest states (${}^{3}B_{1}$ instead of ${}^{1}A_{1}$), but with the cc-pVTZ or cc-pVQZ basis sets, the ${}^{1}A_{1}$ becomes the ground state at the MRCI or MRCI+Q level of theory. Quadratic CI calculations, QCISD(T)/cc-pVQZ, also predict that the ground state is of ${}^{1}A_{1}$ symmetry.